

## Lecture 4 and 5: Constraint Satisfaction Problems (CSPs)

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# Recap: Search

- Search problem:
  - States (configurations of the world)
  - Successor function: a function from states to
  - lists of (state, action, cost) triples; drawn as a graph
  - Start state and goal test

## Search tree:

- Nodes: represent plans for reaching states
- Plans have costs (sum of action costs)

## Search Algorithm:

- Systematically builds a search tree
- Chooses an ordering of the fringe (unexplored nodes)

# What is Search For? Models of the world: single agents, deterministic actions,

- fully observed state, discrete state space
- Planning: sequences of actions
  - The path to the goal is the important thing
  - Paths have various costs, depths
  - Heuristics to guide, fringe to keep backups
- Identification: assignments to variables
  - The goal itself is important, not the path
  - All paths at the same depth (for some formulations)

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CSPs are specialized for identification problems

## **Constraint Satisfaction Problems**

## Standard search problems: State is a "black box": arbitrary data structure

- State is a "black box": arbitrary data struct
  Goal test: any function over states
- Successor function can be anything

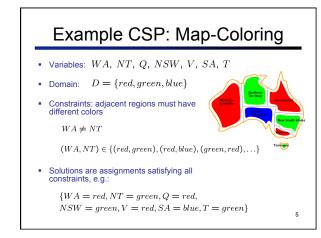
#### Constraint satisfaction problems (CSPs): • A special subset of search problems

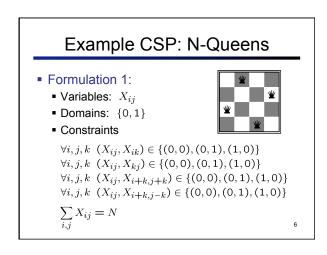
- State is defined by variables X<sub>i</sub> with values from a domain D (sometimes D depends on i)
- Goal test is a set of constraints specifying allowable combinations of values for subsets of variables

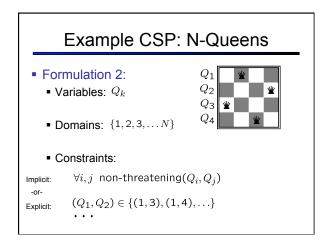
Allows useful general-purpose algorithms with more power than standard search algorithms

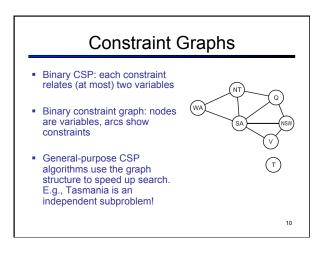
• Simple example of a *formal representation language* 

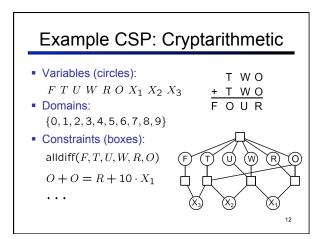


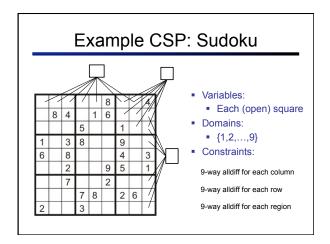


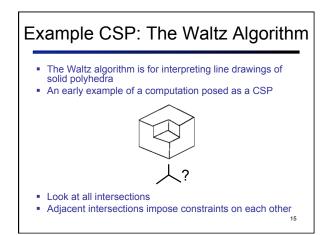


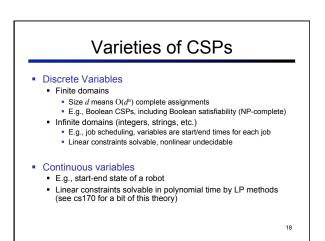












# Varieties of Constraints

## Varieties of Constraints

- Unary constraints involve a single variable (equiv. to shrinking domains):  $SA \neq green$ 

Binary constraints involve pairs of variables;

 $SA \neq WA$ 

 Higher-order constraints involve 3 or more variables: e.g., cryptarithmetic column constraints

### Preferences (soft constraints):

- E.g., red is better than green
- Often representable by a cost for each variable assignment
  Gives constrained optimization problems
- We'll ignore these until we get to Bayes' nets)

- Real-World CSPs
- Assignment problems: e.g., who teaches what class
- Timetabling problems: e.g., which class is offered when and where?
- Hardware configuration
- Transportation scheduling
- Factory scheduling
- Floorplanning
- Fault diagnosis
- Interpretended in the second secon
- Many real-world problems involve real-valued variables...

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# Standard Search Formulation

- Standard search formulation of CSPs (incremental)
- Let's start with the straightforward, dumb approach, then fix it
- States are defined by the values assigned so far
  - Initial state: the empty assignment, {}
    Successor function: assign a value to an unassigned variable
  - Goal test: the current assignment is complete and satisfies all constraints
- Simplest CSP ever: two bits, constrained to be equal

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